

| M.Sc. Course    |   |   |   |          | SC 501T - CLASSICAL MECHANICS & MATHEMATICAL PHYSICS |    |    |           |         |             |
|-----------------|---|---|---|----------|--|----|----|-----------|---------|-------------|
| Teaching Scheme |   |   |   |          | Examination Scheme                                   |    |    |           |         |             |
| L               | T | P | C | Hrs/Week | Theory   |    |    | Practical |         | Total Marks |
|                 |   |   |   |          | MS   | ES | IA | LW        | LE/Viva |             |
| 4               | 1 | 0 | 5 | 5        | 25   | 50 | 25 | --        | --      | 100         |

**COURSE OBJECTIVES**

- ☐ To develop conceptual understanding of the advanced principles of classical mechanics.
- ☐ To appreciate the role of basic methods of classical mechanics towards solutions of various problems of complicated oscillatory systems.
- ☐ To familiarize with the motion of rigid bodies, small oscillations and the mechanics of continuous media.
- ☐ To introduce to the students basic concepts of finite and infinite groups.
- ☐ To learn the Techniques for solving integral equations.
- ☐ To enable students to formulate the Green functions.

**UNIT 1: CANONICAL TRANSFORMATION****15 Hrs.**

Lagrangian and Hamiltonian for central forces, coupled oscillators and other simple systems, Canonical Variables, Gauge transformation, Canonical transformation, condition for transformations to be Canonical. Generators of infinitesimal canonical transformations, Poisson bracket, canonical equations in terms of Poisson bracket notation, Symmetry principles and conservations laws. The Hamilton Jacobi equations, Separation of variables, Action angle variables, Properties of action angle. Centre of mass and laboratory system, Kepler problem.

**UNIT 2: THEORY OF SMALL OSCILLATIONS****15 Hrs.**

Small oscillations, Eigen vectors and eigen frequencies, orthogonality of eigen vectors, normal coordinates, small oscillations of particles on string, normal coordinated and its applications to chain molecules and other problems. Degrees of freedom for a rigid body, Euler angles, Rotating frame, Coriolis force, Foucault's pendulum, Eulerian coordinates and equations of motion for a rigid body, Symmetries and invariance principles, Noether's theorem, motion of a symmetrical top.

**UNIT 3: GROUP THEORY****15 Hrs.**

Elements of finite groups. Representation theory. Group theory: Group, subgroups and classes, cosets, factor groups, normal subgroups, direct product of groups; Examples: cyclic, symmetric, matrix groups, regular n-gon. Mappings: homomorphism, isomorphism, automorphism. Representations: reducible and irreducible representation, unitary representations, Schur's lemma and orthogonality theorems, characters of representation, direct product of representations.

**UNIT 4: INTEGRAL EQUATIONS AND GREEN'S FUNCTIONS****15 Hrs.**

Conversion of ordinary differential equations into integral equations, Fredholm and Volterra integral equations, separable kernels, Fredholm theory, eigen values and eigen functions. Boundary Value Problems: boundary conditions: Dirichlet and Neumann; self-adjoint operators, Sturm-Liouville theory, Green's function, eigenfunction expansion.

**Max. 60 Hrs.****COURSE OUTCOMES**

**After completion of this course students will be able to;**

CO1: Relate with particle mechanics at an advanced level and utilise the foundations to the classical theory of fields.

CO2: Identify and develop the applications in acoustics, molecular spectra and coupled circuits etc.

CO3: Understand the classification of finite groups in Group theory.

CO4: Apply these concepts in various fields, particularly in crystallography/Physics of solids.

CO5: Describe the analytical techniques for solving integral equations and construct Green's functions for many important boundary value problems.

CO6: Determine the classical mechanics formulation for advanced and specialized courses of Physics.

**TEXT/REFERENCE BOOK**

1. Mechanics by Landau and Lifshitz
2. Classical Mechanics by Goldstein
3. Classical Mechanics by Rana and Joag
4. Introduction to Classical Mechanics by Takwale R.G. and P. S. Puranik
5. A.W. Joshi, Elements of Group Theory for Physicists
6. M. A. Armstrong, Groups and Symmetry
7. R. S. Kaushal & D. Parashar, Advanced Method of Mathematical Physics

8. M. Hamermesh, Group Theory and Its Applications to Physical Problems
9. F. Albert Cotton, Chemical Applications of Group Theory
10. G. Arfken, H. Weber, & F. Harris, Mathematical Methods for Physicists
11. W. V. Lovitt, Linear Integral Equations (Dover, 2055).
12. J. Jerri, Introduction to Integral Equations with Applications

| Course Delivery Methods                                     |       |
|---|-------|
| Lecture by use of boards/LCD projectors/OHP projectors      | Yes   |
| Tutorials/Assignments                                       | Yes   |
| Seminars  | Yes   |
| Mini projects/Projects                                      | No    |
| Laboratory experiments/teaching aids                        | No    |
| Industrial/guest lectures                                   | Maybe |
| Industrial visits/in-plant training                         | No    |
| Self- learning such as use of NPTEL materials and internets | Yes   |
| Simulation  | Maybe |

### Course Outcome (CO) Attainment Assessment tools & Evaluation procedure

#### Direct Assessment:

| Assessment Tool     |                          | % Contribution during CO Assessment | Maximum Marks | Exam Duration |
|---------------------|--------------------------|-------------------------------------|---------------|---------------|
| Internal Assessment | Assignment               | 10 %                                | -             | -             |
|                     | Quiz                     | 15%                                 | -             | -             |
| Examianation        | Mid Semester Examination | 25%                                 | 50            | 2 hours       |
|                     | End Semester Examination | 50%                                 | 100           | 3 hours       |

| Assessment Components     | CO1 | CO2 | CO3 | CO4 | CO5 | CO6 |
|---------------------------|-----|-----|-----|-----|-----|-----|
| Mid Sem Examination Marks | YES | YES | NO  | NO  | NO  | YES |
| End Sem Examination Marks | YES | YES | YES | YES | YES | YES |
| Assignment                | YES | YES | YES | YES | YES | YES |

#### Indirect Assessment :

1. Student Feedback on Faculty
2. Student Feedback on Course Outcome

#### Mapping of Course Outcomes onto Program Outcomes

| Course Outcome   | Programme Outcome |     |     |     |     |
|--|-------------------|-----|-----|-----|-----|
|  | PO1               | PO2 | PO3 | PO4 | PO5 |
| CO1: Relate with particle mechanics at an advanced level and utilise the foundations to the classical theory of fields.                            | H                 | H   | M   | L   | M   |
| CO2: Identify and develop the applications in acoustics, molecular spectra and coupled circuits etc.   | M                 | M   | H   | L   | M   |
| CO3: Understand the classification of finite groups in Group theory.   | H                 | M   | M   | L   | L   |
| CO4: Apply these concepts in various fields, particularity in crystallography/Physics of solids.   | M                 | H   | H   | M   | L   |
| CO5: Describe the analytical techniques for solving integral equations and construct Green's functions for many important boundary value problems. | M                 | M   | H   | M   | L   |
| CO6: Determine the classical mechanics formulation for advanced and specialized courses of Physics.  | M                 | H   | H   | L   | M   |

#### Lecture wise Lesson planning Details:

| Week No. | Lect. No. | Unit No. | Topics To be covered                         | CO Mapped | Remarks by Faculty |
|----------|-----------|----------|--|-----------|--------------------|
| 1        | 1         | 1        | Lagrangian for central forces                | CO1, CO2  |                    |
|          | 2         |          | Hamiltonian for central forces               | CO1, CO2  |                    |
|          | 3         |          | coupled oscillators and other simple systems | CO1, CO2  |                    |
|          | 4         |          | Canonical Variables                          | CO1, CO2  |                    |
| 2        | 5         |          | Gauge transformation                         | CO1, CO2  |                    |

|    |   |   |   |               |  |
|----|---|---|---|---------------|--|
|    | 6   |   | Canonical transformation  | CO1, CO2, CO6 |  |
|    | 7   |   | Condition for transformations to be Canonical                                 | CO1, CO2, CO6 |  |
|    | 8   |   | Generators of infinitesimal canonical transformations                         | CO1, CO2, CO6 |  |
| 3  | 9   |   | Poisson bracket   | CO1, CO2, CO6 |  |
|    | 10  |   | Canonical equations in terms of Poisson bracket notation                      | CO1, CO2      |  |
|    | 11  |   | Symmetry principles and conservations laws                                    | CO1, CO2      |  |
|    | 12  |   | The Hamilton Jacobi equations   | CO1, CO2, CO6 |  |
| 4  | 13  |   | Separation of variables   | CO1, CO2      |  |
|    | 14  |   | Action angle variables, Properties of action angle                            | CO1, CO2      |  |
|    | 15  |   | Centre of mass and laboratory system  | CO1, CO2, CO6 |  |
|    | 16  |   | Kepler problem  | CO1, CO2      |  |
| 5  | 17  |   | Small oscillations  | CO1, CO2      |  |
|    | 18  |   | Eigen vectors and eigen frequencies   | CO1, CO2, CO6 |  |
|    | 19  |   | Orthogonality of eigen vectors  | CO1, CO2, CO6 |  |
|    | 20  |   | Normal coordinates  | CO1, CO2, CO6 |  |
| 6  | 21  |   | Small oscillations of particles on string                                     | CO1, CO2      |  |
|    | 22  |   | Normal coordinates and its applications to chain molecules and other problems | CO1, CO2, CO6 |  |
|    | 23  | 2 | Degrees of freedom for a rigid body, Euler angles                             | CO1, CO2, CO6 |  |
|    | 24  |   | Rotating frame  | CO1, CO2      |  |
| 25 | Coriolis force  |   | CO1, CO2  |               |  |
| 26 | Focault's pendulum                                    |   | CO1, CO2  |               |  |
| 7  | 27  |   | Eulerien coordinates and equations of motion for a rigid body                 | CO1, CO2      |  |
|    | 28  |   | Symmetries and invariance principles  | CO1, CO2, CO6 |  |
| 8  | 29  |   | Noether's theorem   | CO1, CO2, CO6 |  |
|    | 30  |   | Motion of a symmetrical top   | CO1, CO2, CO6 |  |
|    | 31  | 3 | Elements of finite groups   | CO3           |  |
|    | 32  |   | Representation theory   | CO3           |  |
| 33 | Group theory: Group, subgroups and classes            |   | CO3   |               |  |
| 34 | Group theory: cosets, factor groups, normal subgroups |   | CO3   |               |  |
| 9  | 35  |   | Direct product of groups  | CO3, CO4      |  |
|    | 36  |   | Examples: cyclic, symmetric   | CO3, CO4      |  |
|    | 37  |   | Matrix groups   | CO3, CO4      |  |
| 10 | 38  |   | Regular n-gon   | CO3, CO4      |  |
|    | 39  |   | Mappings: homomorphism  | CO3, CO4      |  |
|    | 40  |   | Isomorphism, Automorphism   | CO3, CO4      |  |
| 11 | 41  |   | Representations: reducible and irreducible representation                     | CO3, CO4      |  |
|    | 42  |   | Unitary representations   | CO3, CO4      |  |
|    | 43  |   | Schur's lemma and orthogonality theorems                                      | CO3, CO4      |  |
|    | 44  |   | Characters of representation  | CO3, CO4      |  |
| 12 | 45  |   | Direct product of representations   | CO3, CO4      |  |
|    | 46  | 4 | Conversion of ordinary differential equations into integral equations         | CO5           |  |
|    | 47  |   | Fredholm and Volterra integral equations                                      | CO5           |  |
| 48 | Fredholm and Volterra integral equations              |   | CO5   |               |  |
| 13 | 49  |   | Separable kernels   | CO5           |  |
|    | 50  |   | Fredholm theory   | CO5           |  |
|    | 51  |   | Eigen values and eigen functions  | CO5           |  |
| 14 | 52  |   | Boundary Value Problems:  | CO5           |  |
|    | 52  |   | Boundary Value Problems:  | CO5           |  |
|    | 54  |   | Boundary conditions: Dirichlet and Neumann                                    | CO5           |  |
|    | 55  |   | Boundary conditions: Dirichlet and Neumann                                    | CO5           |  |
| 15 | 56  |   | Self-adjoint operators  | CO5           |  |
|    | 57  |   | Sturm-Liouville theory  | CO5           |  |
|    | 58  |   | Green's function  | CO5           |  |

|  |    |  |                         |     |  |
|--|----|--|-------------------------|-----|--|
|  | 59 |  | Green's function        | CO5 |  |
|  | 60 |  | Eigenfunction expansion | CO5 |  |